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# Basic Building Blocks for Analog Design



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This lecture deals with the basis of analog design.

I have decided to prepare the material in a rater "formal" way, deriving almost all the necessary formulas. This was done to try to give you some complete and precise material for future reference.

We will not need to assimilate all the formulas today. The important thing is that we recognize in each formula which are the important parameters and trends.

### Analog design trade-offs



Behzad Razavi, "CMOS Technology Characterization for Analog and RF Design", IEEE JSSC, vol. 34, no. 3, March 1999, p. 268.

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# Analog design methodology





- Single-stage amplifiers
- The differential pair
- The current mirror
- Differential pair + active current mirror
- Operational amplifier (op amp) design

B. Razavi, *Design of Analog CMOS Integrated Circuits*, McGraw-Hill International Edition, 2001. P.R. Gray, P.J. Hurst, S.H. Lewis, R.G. Meyer, *Analysis and Design of Analog Integrated Circuits*, J. Wiley & Sons, 4<sup>th</sup> edition, 2001. R. Gregorian, *Introduction to CMOS Op-Amps and Comparators*, J. Wiley & Sons, 1999. R.L. Geiger, P.E. Allen and N.R. Strader, *VLSI Design Techniques for Analog and Digital Circuits*, McGraw-Hill International Edition, 1990. D.A. Johns and K. Martin, *Analog Integrated Circuit Design*, J. Wiley & Sons, 1997.

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### Outline

Single-stage amplifiers

- Common-source Stage
- Common-drain Stage (Source Follower)
- Common-gate Stage
- Cascode Stage
- Folded cascode Stage
- The differential pair
- The current mirror
- Differential pair + active current mirror
- Operational amplifier (op amp) design



## Common-Source Stage (CSS)



### Small signal model in saturation



The above results could also have been obtained directly from the small signal model

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### **CSS Simulation - DC**





#### Increasing the value of the load resistor to 1 $k\Omega$ we have





## **CSS Simulation – Small Signal**



**R = 1000** Ω

g<sub>m</sub> = 9.6 mS

We inject at the input a sinusoid with frequency 1 kHz, peak to peak amplitude 1 mV AND dc offset = 0.9 V.

The DC offset is important to be in the right bias point.

The input voltage is converted in a current by the transistor and then in a voltage again by the resistor.



A MOS transistor behaves as a small signal resistor when gate and drain are shorted. A transistor in this configuration is referred to as "diode-connected" transistor. The device is always in saturation.

To calculate the impedance of this device we use the small-signal equivalent circuit and a test voltage generator (in red). The ratio between the voltage  $v_x$  applied and the current  $i_x$  gives the impedance.



The calculation show that the impedance is given by the parallel of two resistors,  $1/g_m$  and  $r_0$ .

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### Impedance seen looking into the source.



#### In this case we have three resistances in parallel: $1/g_m$ , $1/g_{mb}$ and $r_0$ .

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### **Diode-connected transistor**

Impedance seen looking into the drain with a resistor R<sub>s</sub> between the source and ground. G, D



Without bulk effect  $(g_{mb})$  and the channel length modulation  $(r_0)$  we would see the series of  $1/g_m$  and  $R_s$ . If  $R_s = 0$  we find again  $1/g_m$ .

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# CSS with diode-connected load



#### The equations above can be obtained in three different ways:

- Using the results found for single transistors (as we have done)
- Starting from the DC equations and doing some mathematics (boring...)
- Using the small signal equivalent circuit (see next slide)

In an N-well CMOS process, the bulk contacts of all the NMOS are connected together to ground (substrate). On the other hand, each bulk contact of the PMOS (each well) can be connected to a desired signal.

# Small signal circuit





### Substituting the NMOS load with a PMOS load, we get rid of the bulk effect.



**Drawbacks of this configuration:** 

- It is difficult to have high gain
- $\mathbf{V}_{\text{out}\_\text{max}} = \mathbf{V}_{\text{DD}} |\mathbf{V}_{\text{GS2}}|$ .
- To have gain,  $(W/L)_2$  is made smaller than  $(W/L)_1$ . This will limit the maximum output voltage, since  $|V_{GS2}|$  will be quite higher than  $V_{T2}$ .



To increase the gain, we can use the output resistance of a transistor. T2 provides the DC current bias to T1, and has a high output impedance. The bias current is determined by V<sub>b</sub>.



The output of the circuit shown is in an undefined state (highimpedance node). This circuit needs therefore an "external system" to fix its output DC bias point (we need a feedback network!).



#### CSS-CSL = Common Source Stage with Current Source Load



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#### **Small signal simulations**



We inject at the input a sinusoid with frequency 1 kHz, peak to peak amplitude 1 mV and DC offset = 0.635 V.

The DC offset is important to be in the right bias point (especially for the output!)

With a current of just 100  $\mu$ A and the same input transistor dimensions as in the case of the CSS with load resistor, we have a gain of –373.

N.B. The output current is smaller than what it should be. The bias point is so critical that the simulator has some problems...

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This circuit is the same as the CSS with Current Source load, but the gate bias of transistor T2 is low enough to make sure that T2 works in the linear region and therefore it behaves as a resistor.



Small signal gain G

$$\mathbf{G} = -\mathbf{g}_{m1} \cdot \frac{1}{\mu_{P} \mathbf{C}_{ox} \frac{\mathbf{W}_{2}}{\mathbf{L}_{2}} \left(\mathbf{V}_{DD} - \mathbf{V}_{b} - \mathbf{V}_{TP}\right)}$$

To have T2 in the linear region, we must have  $V_b < V_{out} - V_{TP}$  (where  $V_{TP}$  is a positive number). If we can not take  $V_b < 0$  V, we can take it = 0 V. In this case we must have  $V_{out} > V_{TP}$ .

# The principal drawback of this circuit is that the small-signal gain depends on many parameters.

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In some applications, the square-law dependence of the drain current upon the gate overdrive voltage introduces excessive non linearity.  $R_s$  "smoothes" this effect since it takes a portion of the gate overdrive voltage. At the limit, for  $R_s >> 1/g_m$ , the small signal gain does not depend on  $g_m$  (and therefore on  $I_{DS}$ ) anymore.

It is interesting to note that the approximated small signal gain (which can be easily calculated with the small signal equivalent circuit) can also be calculated as if  $R_s$  and  $1/g_m$  were two resistors in series.

Small signal gain (approximation)

$$\mathbf{G} = -\frac{\mathbf{R}_{\mathrm{D}}}{\frac{1}{\mathbf{g}_{\mathrm{m}}} + \mathbf{R}_{\mathrm{S}}} = -\frac{\mathbf{g}_{\mathrm{m}}}{1 + \mathbf{g}_{\mathrm{m}}\mathbf{R}_{\mathrm{S}}} \cdot \mathbf{R}_{\mathrm{D}}$$



The approximated small signal voltage gain can also be seen as the product of the small signal equivalent transconductance of the degenerated CS Stage multiplied by the total resistance seen at the output (R<sub>D</sub>).

To calculate the exact small signal voltage gain we need the exact small signal equivalent transconductance and the output resistance of the degenerated CS Stage. Both these quantities can be calculated with the equivalent small signal circuits.





### Calculation of the output resistance of the degenerated CS Stage.



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### Exact small signal gain of the degenerated CS Stage.



Exercise: try to obtain the same equation with the complete small signal circuit

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# Source Follower (SF)

The analysis of the Common Source Stage (CSS) with current source load demonstrated that to have a high voltage gain we have to have a high load impedance. If we want to use a CSS to drive a low impedance load, we have to put a "buffer" between the CSS and the load. The simplest buffer is the Source Follower (also called Common Drain Stage).

> How do we obtain the small signal gain? We could use the small signal equivalent circuit or we can be clever and reuse what we have seen up to now!

$$\mathbf{G} = \frac{\mathbf{V}_{\text{out}}}{\mathbf{V}_{\text{in}}} = \mathbf{g}_{\text{m}} \cdot \left( \mathbf{R}_{\text{S}} \, / / \frac{1}{\mathbf{g}_{\text{m}} + \mathbf{g}_{\text{mb}} + 1 / \mathbf{r}_{0}} \right)$$

$$\mathbf{G} = \frac{\mathbf{g}_{m}}{\mathbf{g}_{m} + \mathbf{g}_{mb} + \frac{1}{\mathbf{r}_{0}} + \frac{1}{\mathbf{R}_{s}}} = \frac{\mathbf{g}_{m} \cdot \mathbf{R}_{s}}{1 + (\mathbf{g}_{m} + \mathbf{g}_{mb}) \cdot \mathbf{R}_{s}}$$

The gain of our buffer is never one! It is, in the best case, 1/n

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V<sub>DD</sub>



The Source Follower with a resistor is highly non linear, since the drain current in T1 is a strong function of the input DC level. We can therefore replace the resistor with a current source.

$$\mathbf{G}_{\text{SF}_{\text{NMOS}}} = \mathbf{g}_{\text{m1}} \cdot \left( \mathbf{r}_{02} \, / / \frac{1}{\mathbf{g}_{\text{m1}} + \mathbf{g}_{\text{mb1}} + 1/\mathbf{r}_{01}} \right) = \frac{\mathbf{g}_{\text{m1}}}{\mathbf{g}_{\text{m1}} + \mathbf{g}_{\text{mb1}} + 1/\mathbf{r}_{01} + 1/\mathbf{r}_{02}}$$

The gain is in this case close to 1/n (still not 1...). The circuit is still non linear due to the body effect (non linear dependence of  $V_{T1}$  upon the source potential). This can be solved using a PMOS Source Follower, in which both the transistors have the body (well) connected to the source. In this case, we have:

$$G_{\text{SF}_PMOS} = g_{m1} \cdot \left( r_{02} \, / / \frac{1}{g_{m1} + 1/r_{01}} \right) = \frac{g_{m1}}{g_{m1} + 1/r_{01} + 1/r_{02}}$$

#### The gain can be in this case very close to one!

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### Source Follower drawbacks

$$G = g_{m1} \cdot \left( \frac{R_{L}}{r_{02}} \frac{1}{g_{m1} + 1/r_{01}} \right) = \frac{g_{m1}}{g_{m1} + 1/r_{01} + 1/r_{02} + 1/R_{L}}$$
$$G \approx \frac{g_{m1}}{g_{m1} + 1/R_{L}} = \frac{R_{L}}{R_{L} + 1/g_{m}}$$

If the source follower has to drive a low impedance, we risk to have a gain which is significantly smaller than one. Another important drawback is that source followers shift the signal by one  $V_{GS}$ . This is a drawbacks especially in low voltage circuit, where this causes a limitation in the voltage headroom. On the other hand, if the power supply voltage is high enough, source followers can be used as voltage level shifters.



In Common-Source Stages and Source Followers the input signal is applied to the gate. We can also apply it to the source, obtaining what is called a Common-Gate Stage (CGS)

$$V_{DD}$$

$$R_{out} = R_{out\_CGS} // R_{D}$$

$$R_{out\_CGS} = r_{0}$$

$$R_{in} = \frac{1 + R_{D} / r_{0}}{g_{m} + g_{mb} + r_{0}} = \frac{R_{D} + r_{0}}{1 + (g_{m} + g_{mb}) \cdot r_{0}} \rightarrow EXERCISE!$$

$$V_{b} = V_{out}$$

$$G = \frac{R_{out}}{R_{in\_R_{D}=0}} = (r_{0} // R_{D}) \cdot (g_{m} + g_{mb} + 1/r_{0})$$

$$G = \frac{R_{D}}{R_{in}} = R_{D} \cdot \frac{r_{0} \cdot (g_{m} + g_{mb}) + 1}{R_{D} + r_{0}} \approx g_{m} \cdot n \cdot R_{D}$$

The input impedance of a CGS is relatively low, but this only if the load impedance in low. The gain is slightly higher to the one of a CSS, since we apply the signal to the source. N.B. We have calculated the small signal gain using 2 different methods (red and blue). The results are identical!

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 $\mathbf{V}_{\mathrm{DD}}$ 

 $\mathbf{V}_{\mathsf{out}}$ 

 $\mathbf{V}_{\mathrm{in}}$ 

With the results obtained, it is now very easy to study the most "general" case, which includes the impedance  $R_s$  of the signal source, the channel modulation effect and the bulk effect. Let's call  $R_{in}$  the resistance seen by the ideal voltage source.

$$R_{in} = R_{s} + \frac{R_{D} + r_{0}}{1 + (g_{m} + g_{mb}) \cdot r_{0}} \qquad \qquad \frac{v_{in}}{R_{in}} \cdot R_{D} = v_{out}$$
$$G = \frac{v_{out}}{v_{in}} = \frac{R_{D}}{R_{in}} = R_{D} \cdot \frac{1 + (g_{m} + g_{mb}) \cdot r_{0}}{R_{s} \cdot [1 + (g_{m} + g_{mb}) \cdot r_{0}] + R_{D} + r_{0}}$$

This result is very similar to the one of a Common Source Stage with source degeneration. The gain here is still slightly higher due to the body effect. It is now also easy to calculate the resistance seen into the output.

$$\mathbf{R}_{out} = \mathbf{R}_{D} // \mathbf{R}_{out\_CSS\_deg}$$
$$\mathbf{R}_{out\_CSS\_deg} = \mathbf{r}_{0} + \mathbf{R}_{S} + (\mathbf{g}_{m} + \mathbf{g}_{mb}) \cdot \mathbf{r}_{0} \mathbf{R}_{S}$$



Cascode Stage (CascS)

The "cascade" of a Common-Source Stage (V-I converter) and of a Common-Gate Stage is called a "Cascode".





One nice property of the cascode stage can be discovered looking at the resistance seen in the drain of T2. This is quickly done if we look at T2 as a Common-Source Stage with a degeneration resistor =  $r_{01}$ .



The disadvantage of the cascode configuration is that the minimum output voltage is now the sum of the saturation voltages of T1 and T2. It must therefore be used with care in low voltage circuits.

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To fully profit of the high output impedance of the cascode stage, it seems natural to load it with a high impedance load, like a current source.



$$\mathbf{R}_{\text{out}\_\text{CascS}} = \mathbf{r}_{01} + \mathbf{r}_{02} + (\mathbf{g}_{m2} + \mathbf{g}_{mb2}) \cdot \mathbf{r}_{01} \mathbf{r}_{02}$$

 $\mathbf{R}_{out} = \mathbf{R}_{out\_CascS} // \mathbf{r}_{03}$ 

$$\mathbf{G} \approx -\mathbf{g}_{m1}\mathbf{R}_{out}$$

If  $r_{03}$  is not high enough, we can use the cascode principle to boost the output impedance of the current source as well.

N.B. Remember that the DC output level here is not well defined, and that we will need a feedback loop.

# Folded Cascode Stage (FCascS)



This solution is has a lower output impedance than the standard CascS and consumes more current for the same performance.

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### Outline

- Single-stage amplifiers
- The differential pair
  - Differential signal advantages
  - The differential pair
    - Common Mode Analysis
    - Large Signal Analysis
    - Small Signal Analysis
    - Common Mode Rejection Ratio (CMMR)
  - Differential pair with MOS loads
  - Differential Pair Mismatch
- The current mirror
- Differential pair + active current mirror
- Operational amplifier (op amp) design



A single-ended signal is defined as a signal measured with respect to a fixed potential (usually, ground).

A differential signal is defined as a signal measured between two nodes which have equal and opposite signal excursions. The "center" level in differential signals is called the Common-Mode (CM) level.

The most important advantage of differential signals over single-ended signals is the much higher immunity to "environmental" noise.

As an example, let's suppose to have a disturbance on the power supply.



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The Common-Mode disturbances disappear in the differential output.




# Differential Pair (DP)



The current source has a very important function, since it makes the sum of the currents in the two branches  $(I_1 + I_2 = I_{SS})$  independent from the input common mode voltage.

 $\mathbf{V}_{\text{out,CM}} = \mathbf{V}_{\text{DD}} - \mathbf{R}_{\text{D}} \cdot \frac{\mathbf{I}_{\text{SS}}}{2}$ 

The output common mode voltage is then given by:

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**Differential Pair** 



To better understand what can be the maximum voltage excursion of the input, we substitute the ideal current source with a real one.



With the basic transistor equations, some patience and some mathematics we can obtain the equation for the plot shown.



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Deriving the current difference as a function of the input voltage difference we obtain the transconductance  $G_m$  of the differential pair.





# DP small signal gain

From the transconductance  $G_m$  of the differential pair when the differential stage is balanced ( $\Delta v_{in} = 0$ ), we obtain the small signal gain G.

$$G_{m} = \sqrt{\frac{2\beta}{n} \frac{I_{ss}}{2}} \qquad \Delta V_{out} = -R_{D} \cdot \Delta I = -R_{D} \cdot G_{m} \cdot \Delta V_{in}$$
$$G = \frac{\Delta V_{out}}{\Delta V_{in}} = -R_{D} \cdot \sqrt{\frac{2\beta}{n} \frac{I_{ss}}{2}}$$

The term circled in red looks suspiciously familiar to us...

It is the transconductance in strong inversion of a transistor carrying a current  $I_{ss}/2$  ! So we can write

$$\mathbf{G} = -\mathbf{R}_{\mathsf{D}} \cdot \mathbf{g}_{\mathsf{m}}$$

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# DP small signal gain

Now that we know it, is is quite obvious to recognize it looking again at the circuit schematic.



We can see the circuit as two common source stages with degenerated resistor, and superimpose the effects.

Or, even better, we can realize that the point P is (ideally) AC grounded.

$$\mathbf{v}_{out1} = -\mathbf{g}_{m} \cdot \mathbf{R}_{D} \cdot \mathbf{v}_{in1}$$
$$\mathbf{v}_{out2} = -\mathbf{g}_{m} \cdot \mathbf{R}_{D} \cdot \mathbf{v}_{in2}$$
$$_{out1} - \mathbf{v}_{out2} = -\mathbf{g}_{m} \cdot \mathbf{R}_{D} \cdot (\mathbf{v}_{in1} - \mathbf{v}_{in2})$$

V



# DP Common Mode gain

We have seen that ideally in a differential pair the output voltage does not depend on the common mode input voltage. But in fact the non infinite output impedance  $r_{03}$  of the current source has an influence, since the point P do not behave as an AC ground anymore. The symmetry in this circuit suggests that we can see it as two identical half circuits in parallel. This makes the analysis much easier.





The variation of the common mode output voltage with the common mode input voltage is generally small and not so worrying. MUCH MORE concerning is when we have a differential output as a consequence of a common mode variation at the input! This can happen if the circuit is not fully symmetric (mismatch!). Let's call  $G_{CM-DM}$  the gain of this common-mode to differential-mode conversion. A difference in the transconductances of the two transistors, for example, would give:

$$\mathbf{G}_{\mathsf{CM}-\mathsf{DM}} = \frac{\Delta \mathbf{g}_{\mathsf{m}} \cdot \mathbf{R}_{\mathsf{D}}}{\left(\mathbf{g}_{\mathsf{m1}} + \mathbf{g}_{\mathsf{m2}}\right)\mathbf{r}_{\mathsf{03}} + \mathbf{1}}$$

We see that it is essential to have a good current source (very high  $r_{03}$ ). To make possible a meaningful comparison between different differential circuit, we want to compare the undesirable differential output given by a common mode input variation and the wanted differential output given by a differential input.

 $\mathbf{CMRR} = \left| \frac{\mathbf{G}}{\mathbf{G}_{\mathsf{CM-DM}}} \right|$ 

We define the Common Mode Rejection Ratio (CMRR) as:

Taking into account ONLY the transconductance mismatch, we obtain  $CMRR \approx \frac{g_m}{\Delta g_m} (1 + 2g_m r_{03})$ 

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To analyze the two circuits we can now make use of the half-circuit concept and profit from all the results obtained up to now.

$$\mathbf{G} = -\mathbf{g}_{mN} \left( \frac{1}{\mathbf{g}_{mP}} // \mathbf{r}_{0N} // \mathbf{r}_{0P} \right) \approx -\frac{\mathbf{g}_{mN}}{\mathbf{g}_{mP}}$$

$$\mathbf{G} = -\mathbf{g}_{\mathsf{mN}} \big( \mathbf{r}_{\mathsf{0N}} \, / / \, \mathbf{r}_{\mathsf{0P}} \big)$$







### **Cascode Differential Pair**

And, of course, the gain can be boosted using common-gate stages.



$$\mathbf{G} \approx -\mathbf{g}_{m1} (\mathbf{g}_{m3} \mathbf{r}_{03} \mathbf{r}_{01} // \mathbf{g}_{m5} \mathbf{r}_{05} \mathbf{r}_{07})$$

Cascode stages were used a lot in the past, when the supply voltages were relatively high (few volts).

In deep submicron technologies they are used with more care.

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#### The two transistors have the same drain current





### Outline

- Single-stage amplifiers
- The differential pair
- The current mirror
  - Standard Current Mirror
  - Cascode Current Mirror
  - Low-voltage Cascode Current Mirror
  - Current Mirror Output Impedance
  - Current Mirror Mismatch
- Differential pair + active current mirror
- Operational amplifier (op amp) design



# Current mirror (CM)



To have an exact replica of the reference current, we have to make the transistor identical AND they must have the same  $V_{DS}$ . When this is not possible, choosing long devices reduces the effect of  $\lambda$ . Precise current ratios can be obtained playing with the ratio between the transistor widths (not the lengths!).

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# **Current mirror simulation**

0.25  $\mu m$  technology, V\_{DD} = 2.5 V, I\_{REF} = 100  $\mu A,$  W\_R = W\_1 = 100  $\mu m,$  L\_R = L\_1





# Cascode current mirror (CCM)



 $V_{G3}$  must be fixed so that  $V_{D1} = V_{D2}$ . Making  $L_1 = L_2$  and therefore having  $\lambda_1 = \lambda_2$ , we obtain that the current  $I_3$  practically does not depend on the voltage  $V_{D3}$ . Of course, all the devices must be in saturation (the circuit is

not suitable for low voltage applications).

$$\mathbf{I}_{3} = \mathbf{I}_{\mathsf{REF}} \cdot \frac{\mathbf{W}_{2} / \mathbf{L}_{2}}{\mathbf{W}_{1} / \mathbf{L}_{1}}$$
$$\Delta \mathbf{V}_{\mathsf{D2}} \approx \frac{\Delta \mathbf{V}_{\mathsf{P}}}{(\mathbf{g}_{\mathsf{m3}} + \mathbf{g}_{\mathsf{mb3}}) \cdot \mathbf{r}_{\mathsf{03}}}$$

Important:  $L_3$  can be different from  $L_1$  and  $L_2$ .

How do we fix  $V_{G3}$  so that  $V_{D1} = V_{D2}$ ?

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# Cascode current mirror (CCM)



Transistor 4 does the job here! Transistors 1 & 2 decide the current ratio. Transistors 3 & 4 fix the bias  $V_{D1} = V_{D2}$ . These results are valid even if transistors 3 & 4 suffer from body effect.  $\mathbf{I}_{3} = \mathbf{I}_{\mathsf{REF}} \cdot \frac{\mathbf{W}_{2} / \mathbf{L}_{2}}{\mathbf{W}_{1} / \mathbf{L}_{4}}$  $W_{2}/L_{2}$   $W_{3}/L_{3}$ 

$$\frac{1}{W_1/L_1} = \frac{1}{W_4/L_4}$$

The problem of this current mirror is that  $V_{D3} > V_{DS3} + V_{GS2}$ .

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0.25  $\mu m$  technology, V\_{DD} = 2.5 V, I\_{REF} = 100  $\mu A$ 







The main difference of this current mirror compared to the standard cascode current mirror is that here we can lower the voltages  $V_{D1}$  and  $V_{D2}$  to the limit of the saturation of transistors T1 and T2.

$$\mathbf{I}_3 = \mathbf{I}_{\mathsf{REF}} \cdot \frac{\mathbf{W}_2 / \mathbf{L}_2}{\mathbf{W}_1 / \mathbf{L}_1}$$

$$\frac{W_2 / L_2}{W_1 / L_1} = \frac{W_3 / L_3}{W_4 / L_4}$$

#### The minimum output voltage ( $V_{D3}$ ) here is just two saturation voltages.

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0.25  $\mu m$  technology, V\_{DD} = 2.5 V, I\_{REF} = 100  $\mu A$ 



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# Low Voltage CCM simulation (2)





# Current mirrors: comparison



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# Current mirror output impedance





#### The two transistors have the same gate voltage



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### Outline

- Single-stage amplifiers
- The differential pair
  - The current mirror
- Differential pair + active current mirror
  - > Common mode, small signal and large signal analysis
  - Noise
  - Offset
- Operational amplifier (op amp) design



# Differential Pair + Active CM

Current mirrors can also process a signal, and they can therefore be used as active elements. A differential pair with an active current mirror is also called a differential pair with active load. The current mirror here has also the important role to make a differential to single-end conversion!



**Common Mode Analysis** 

$$\mathbf{V}_{\text{in,CM}\_\text{min}} = \mathbf{V}_{\text{GS1}} + \mathbf{V}_{\text{DS}\_\text{SAT5}}$$

$$\mathbf{V}_{\text{in,CM}_{\text{max}}} = \min\left(\mathbf{V}_{\text{DD}} - \mathbf{V}_{\text{GS3}} + \mathbf{V}_{\text{T1}}, \mathbf{V}_{\text{DD}}\right)$$

**Maximum output excursion** 

$$\mathbf{V}_{\mathsf{out\_min}} = \mathbf{V}_{\mathsf{DS\_SAT2}} + \mathbf{V}_{\mathsf{DS\_SAT5}}$$

$$\mathbf{V}_{\text{out}\_\text{max}} = \mathbf{V}_{\text{DD}} - \mathbf{V}_{\text{DS}\_\text{SAT4}}$$



### Differential Pair + Active CM

Let's now calculate the small-signal behavior, neglecting the bulk effect for simplicity. The circuit is NOT symmetric, and therefore we can not use the halfcircuit principle here. As a first approximation, we can consider the common sources of the input transistors as a virtual ground. The small-signal gain G can be seen as the product of the total transconductance of the stage and of the

output resistance.



 $i_{out} = -g_{m1} \frac{v_{in}}{2} - g_{m2} \frac{v_{in}}{2} = -g_{m1,2} \cdot v_{in}$ 

$$\mathbf{G}_{\mathrm{m}} = \frac{\mathbf{I}_{\mathrm{out}}}{\mathbf{V}_{\mathrm{in}}} = -\mathbf{g}_{\mathrm{m1,2}}$$

 $\mathbf{G} = \mathbf{G}_{m} \cdot \mathbf{R}_{out}$ 

$$R_{out} = r_{02} // r_{04}$$

$$\mathbf{G} = -\mathbf{g}_{m1,2} \left( \mathbf{r}_{02} \, / / \, \mathbf{r}_{04} \right)$$



In reality, the current source is not ideal, and this has an effect on the gain we have just calculated. This effect is in general negligible. What is not negligible is the effect of  $r_{05}$  on the common mode gain. For a common mode input signal the circuit can be seen symmetric! It can be shown that even for a perfectly symmetric circuit (no mismatch) a CM signal at the input ( $\Delta v_{in,CM}$ ) generates an unwanted signal at the output ( $\Delta v_{out}$ ).





### Noise in a DP + Active CM





### Noise in a DP + Active CM





### Offset of a DP + Active CM



#### **RANDOM OFFSET (WORST CASE)**

$$\mathbf{V}_{off} = \Delta \mathbf{V}_{T1,2} + \frac{\mathbf{I}}{\mathbf{g}_{m1,2}} \left( \frac{\Delta \beta_{1,2}}{\beta_{1,2}} + \frac{\Delta \beta_{3,4}}{\beta_{3,4}} + \frac{\mathbf{g}_{m3,4}}{\mathbf{I}} \Delta \mathbf{V}_{T3,4} \right)$$

#### SYSTEMATIC OFFSET

The difference in the drain voltages of T1 and T2 gives origin a difference in the DC currents in the two branches.

#### **"COMMON MODE" OFFSET**

As we have already seen, a common mode signal at the input gives a non zero output voltage signal.



List of Acronyms

- CSS: Common-Source Stage
- CSS-CSL: Common-Source Stage with Current Source Load
- SF: Source Follower (also called Common-Drain Stage)
- CGS: Common-Gate Stage
- CascS: Cascode Stage = CSS + CGS
- FCascS: Folded Cascode Stage
- DP: Differential Pair
- CM: Current Mirror
- CCM: Cascode Current Mirror
- LVCCM: Low-Voltage Cascode Current Mirror
- CMRR: Common Mode Rejection Ratio



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### Outline

- Single-stage amplifiers
- The differential pair
- The current mirror
- Differential pair + active current mirror
  - Frequency analysis of an amplifier
  - Operational amplifier (op amp) design
    - Single-stage op amps
    - Two-stage op amps



# **Op-amp application examples**



#### The above equations are valid only if the gain of the op-amp is very high!

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# Single-stage Op Amp



Several different solutions can be adopted to make a Single-stage amplifier. If high gains are needed, we can use, for example, cascode structures.

With single-stage amplifiers it is difficult to obtain at the same time high gain and voltage excursion, especially when other characteristics are also required, such as speed and/or precision.

Two-stage configurations in this sense are better, since they decouple the gain and voltage swing requirements.



# Two-stage Op Amp



The second stage is very often a CSS, since this allows the maximum voltage swing.

The output voltage swing in this case is V<sub>DD</sub> - |2V<sub>DS\_SAT</sub>|

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## Two-stage Op Amp

 $\mathbf{G} = \left\{ \mathbf{g}_{m1,2} \left[ (\mathbf{g}_{m3,4} + \mathbf{g}_{mb3,4}) \mathbf{r}_{03,4} \mathbf{r}_{01,2} \right] // \left[ (\mathbf{g}_{m5,6} + \mathbf{g}_{mb5,6}) \mathbf{r}_{05,6} \mathbf{r}_{07,8} \right] \right\} \cdot \mathbf{g}_{m9,10} \left( \mathbf{r}_{09,10} // \mathbf{r}_{011,12} \right)$ 



To increase the gain, we can again make use, in the first stage, of cascode structures.



## Two-stage Op Amp



Two-stage op amps can also have a single-ended output. In this case, we kept the differential behavior of the first stage, and is the current mirror T7-T8 which does the differential-to-single ended conversion.

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